

ECS 452 Additional Examples for Section 5.1

1. Suppose the generator matrix of a linear code is given by

$$\mathbf{G} = \begin{pmatrix} 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{pmatrix}$$

- a. Find the codeword for the message $\mathbf{b} = [1 \ 0 \ 0]$

- b. Find the codeword for the message $\mathbf{b} = [0 \ 1 \ 1]$

2. Suppose the generator matrix of a linear code is given by

$$\mathbf{G} = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 \end{bmatrix}$$

- a. Find the codeword for the message $\mathbf{b} = [1 \ 0 \ 0 \ 0]$

- b. Find the codeword for the message $\mathbf{b} = [0 \ 1 \ 1 \ 0]$

3. Suppose the generator matrix of a linear code is given by

$$\mathbf{G} = \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 \end{bmatrix}$$

Find the complete codebook of this code.